# Family, Community and Long-Term Earnings Inequality ${ }^{\text {s }}$ 

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#### Abstract

Correlations between the earnings of siblings reflect shared family and community background, but evidence is mixed on the relative magnitudes of these influences. In this paper, we develop a model of multi-person earnings dynamics and decompose for the first time the sibling correlation of earnings into family, neighborhood and school effects, taking into account sorting of families into communities. Using administrative data on the Danish population we link individuals to their siblings, schoolmates and teenage neighbors to measure the relative importance of each factor on long-term earnings. We find that: (1) family is by far the most relevant factor that shapes long-term earnings; (2) the contribution of neighborhoods and schools on long-term earnings is overestimated if the family component is ignored, and becomes negligible and not significantly different from zero by age 30; and (3) the importance of family declines over the life-cycle.


Keywords: Sibling correlations; Neighborhoods; Schools; Life-cycle earnings; Inequality JEL codes: D31, J62

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## 1. Introduction

Understanding the relative importance of factors that shape one's earnings potential is crucial for identifying the driving forces of existing inequalities and for interventions that aim to reduce them. Family and community background are generally considered as the two most important factors that determine socioeconomic outcomes, including earnings. Families can affect earnings by transmitting abilities, preferences and resources, while communities can determine earnings through neighborhood quality, school quality and peers. The existing evidence for the effect of community background on earnings is mixed with both positive (Page and Solon, 2003; Raaum et al., 2006; Chetty et al, 2015), or no effects (e.g. Oreopoulos, 2003). In this past research, community background has been associated with neighborhoods, while the role of school quality and its relative importance with respect to neighborhoods remains unknown. We also know very little about the importance of each of these three factors (family, neighborhood and schools) on long-term earnings.

In this paper, using administrative data on the full population of Denmark, we exploit information on the joint earnings dynamics of siblings, neighbors and schoolmates to measure the relative importance of families, neighborhoods and schools on long-term earnings. We develop a model of multi-person earnings dynamics with family, school and neighborhood effects, and use the parameter estimates to directly decompose for the first time the sibling correlation of permanent earnings into these three components, taking into account sorting of families into communities.

The correlation of sibling earnings, which measures the fraction of the variation in permanent earnings that can be attributed to both observed and unobserved factors shared by siblings during childhood, has been widely used in the literature as a broad measure of the influence of both family and community background (for reviews see Solon, 1999; Björklund and Jännti, 2009; Black and Devereux, 2011). The main is that families sort into communities
so when observing only siblings in the data the community effects are not separable from family effects.

In our setting, thanks to the extraordinary information available in the Danish registers, we observe not only siblings but also teenage neighbors and schoolmates so we are able to separately identify the influence of families, neighborhoods and schools on permanent earnings. While siblings share both the family and the community, neighbors and schoolmates share only their specific community factor (neighborhood or school, respectively) but do not share the family. Moreover, we observe individuals over their life-cycle, which ensures we can address measurement error biases and estimate the influence of the determinants of permanent earnings in the very long run (up to age 51). Following Baker and Solon (2003), we exploit this rich information within a model of earnings dynamics which we extend it to account for the joint earnings dynamics of multiple persons. With the proposed model we jointly decompose the sibling correlation of earnings over the life-cycle into the three components of interest - family, neighborhood and school - taking into account sorting of families across neighborhoods and schools. ${ }^{1}$

We find that the family is the most important factor that shapes long-term earnings. The correlations of earnings between neighbors and schoolmates are measured around zero on average over the life-cycle. Ignoring the family component and estimating the model only considering the community factor leads to an overestimation of the influence of neighborhoods and schools on long-run earnings. This suggest that by jointly estimating the family and community factors within our model we are able to take into account the sorting that would otherwise lead to biased estimates of the community influence. Although on average the community effects are measured around zero over the life-cycle, there is some contribution from community effects at the beginning of the life cycle, but this becomes

[^1]negligible and not significantly different from zero by age 30. Finally, we find that the importance of family declines over the life-cycle.

The paper is structured as follows. In Section 2 we sketch the theoretical background and discuss the related literature. In Section 3 we describe the data and the way we identify neighbors and schoolmates, while in Section 4 we present descriptive statistics on earnings of siblings and peers. In Section 5 we develop the econometric model for assessing the relative importance of families, schools and neighborhoods within the sibling correlation, based on the joint analysis of life-cycle earnings for brothers, schoolmates and neighbors. The main results are presented in Section 6 together with a sensitivity analysis and evidence of heterogeneity by family, neighborhood and school types. We conclude in the last section.

## 2. Background and Related Literature

The aim of this paper is to identify the determinants of long-term earnings inequality and, in particular, the extent to which earnings inequality can be explained by differences in family and social background. Based on the analysis by Becker and Tomes (1979), families by transmitting abilities, preferences and resources to their offspring can influence their human capital investment and, therefore, their earnings. Community background can also influence individual outcomes through institutions such as the school and its quality (e.g. Hanushek, 2006), or through the quality of neighborhood, or peer influences, social norms and role models in the neighborhood (e.g. Wilson, 1987). Differences between families in the availability of these traits, resources and exposure to the community environment would lead to differences in human capital accumulation. According to human capital theory, differential investments of human capital would generate heterogeneity of both initial earnings and earnings growth (Mincer, 1958, Ben-Porath, 1967). More specifically, these models predict that heterogeneous investments in human capital induce a negative correlation between initial earnings and earning growth rates. That is because investors trade off lower initial earnings
with higher earnings growth in later parts of their working life. The prediction is that inequality of earnings should follow a u-shape pattern by age because earnings profiles would exhibit a cross-over property.

The correlation of sibling earnings or other outcomes has been used as a way of measuring the joint influence of family and community background shared by the siblings (see the reviews in Solon, 1999; Björklund and Jännti, 2009; and Black and Devereux, 2011). To disentangle family from community effects, where community is defined by the neighborhood, studies have compared the correlation of sibling earnings with the correlation of earnings among unrelated neighbors (Oreopoulos, 2003; Page and Solon, 2003; Raaum et al. 2006). The idea is that while siblings share both the family and the neighborhood, unrelated neighbors share only the neighborhood but not the family. Following this approach, Page and Solon (2003) using data from the PSID, and Raaum et al. (2006) using administrative data from Norway find a substantial or non-negligible effect of neighborhoods on earnings. However, the estimate of neighborhood effect is recognized to be an upper bound because of non-random sorting of families into neighborhoods, which leads to a positive correlation between the two factors. The correlation of neighbors' earnings will measure the proportion of variance due only to neighborhood effects if sorting is non-random. Oreopoulos (2003) addresses sorting by exploiting quasi-random assignment of families to public housing projects in Toronto finding a zero influence of neighborhood quality in the total variance of income and wages, while the effect is positive and significant for the whole population of Toronto where assignment to neighborhoods is not random.

Outside the sibling correlation literature, the evidence from social experiments such as the Moving to Opportunity experiment, which offered to eligible families living in high poverty neighborhoods randomly a voucher to move to better neighborhoods, suggests that changes in neighborhood quality had on average little impact on economic outcomes including earnings (e.g. Ludwig et al., 2013). However, Chetty et al. (2015) using
administrative data from tax returns find that moving to a lower-poverty neighborhood improves earnings in their mid-twenties for children who were below age 13 when their families moved. Gould, Lavy and Paserman (2011) using the airlift of Yemenite immigrants as a natural experiment find long term effects of early childhood environment on education but not on other economic outcomes. ${ }^{2}$

Related to the school literature and, in particular, the effect of school quality on earnings the evidence is generally mixed. Card and Krueger (1992) exploit variation of school quality across cohorts within U.S. regions and find that higher quality (a lower pupil/teacher ratio) increases the rate of return to schooling and earnings. The evidence of the effect of pupil/teacher ratio in the UK, however, is found to be insignificant (Dearden et al. 2002). Linking the data from the Tennessee STAR experiment, which randomly assigned students and their teachers to classrooms of different size with tax return data, Chetty et al. (2011) find no effect of class size on earnings at age 27, but they find a positive effect of teacher quality. More recently, using Swedish data and exploiting a maximum class size rule, Fredriksson et al. (2013) find a positive effect of smaller class size on adult earnings at ages 27 to 42 .

In this study, we contribute to these different strands of the literature by developing a unified framework which allows decomposing directly the influence of families, neighborhoods and schools on long-term earnings inequality taking into account sorting of families into communities. The two distinguishing features of this study are: (1) that we provide the first decomposition between all three factors jointly, and (2) that we can estimate these effects in the very long run (up to age 51), while most studies measure outcomes up to age 30.

[^2]
## 3. Data

We use data from administrative registers of the Danish population. The civil registration system was established in 1968 and everyone resident in Denmark then and since has been registered with a unique personal identification number which has subsequently been used in all national registers enabling accurate linkage. In outline, construction of our dataset proceeds as follows: First we create our sample of brothers by sampling fathers and finding their first and second born sons. Second we find other members of the sons' teenage communities by linking them to their schoolmates and neighbors.

In order to establish our dataset of brothers we consider first sons born 1960-1982 and second sons born 1962-1982. This selection is because of completeness of registered parentage and the small number of first sons observed born before $1960 .{ }^{3}$ Next we link our sampled brothers to their teenage communities (schools and neighborhoods). School attendance rules were such that pupils should start in first grade in the August of the calendar year they turn seven. The national pupil database was established along with a school reform that made attendance in 9th grade compulsory from the academic year beginning August 1973. ${ }^{4}$ The database links pupils to the schools they are enrolled from 8th grade and above. School identifiers are consistent over time and schools are classified according to whether they are publicly run ( $77 \%$ of schools and $89 \%$ of pupils in our estimation sample) or privately run, and whether they are exclusively for pupils with special educational needs ( $10 \%$ of schools and $1 \%$ of pupils in our gross sample). ${ }^{5}$

[^3]We link pupils to schoolmates on 31 October of the calendar year they turn 15, which is in the academic year they would normally attend 9 th grade. ${ }^{6}$ During our sample period, pupils were assigned to public schools on a catchment area basis according to place of residence. Our sample contains 2657 schools with males attending 9th grade. They have on average 14.7 school mates. Primary and lower secondary education usually takes place in the same school and most pupils attend the same school for all grades. For example, in 2007, the first year that the pupil database was extended down to grade $1,90 \%$ of pupils in grades 1-8 were enrolled in the same school the following year. Due to the organization of primary and secondary schools largely as a single unit, there is likely to be less pupil mobility between schools than in other countries. The institutional setting makes Denmark a good place to look for school effects, because of the coherence of the schoolmate group.

Address of residence is obtained from the central person register which was established in 1968. Individuals are required to report changes of address to the municipal person register within two weeks. Precision of historical address registration has improved over time and we use parish of residence which is recorded consistently throughout our sample period. Similar to schools, our census point is 31 October of the calendar year a male turns 15. There are 1905 parishes covering on average an area of $22.4 \mathrm{~km} \wedge 2$ and containing 19.4 teenage neighbors.

For both brothers and for peers we use pre-tax annual labor earnings measured in 2005 prices. Table 1 presents the cohorts we include in the sample, the first year we start observing their earnings, the total number of year observed, and the last age observed. Following Baker and Solon (2003) we group data in 2-years birth cohorts and we compute age by imputing each cohort with its earlier year of birth. The selection of birth cohorts ensures that each cohort is observed for at least 6 years (cohort 1982) up to 28 years (cohort 1960).

[^4]
## 4. Descriptive statistics on earnings of siblings and peers

In this section we provide a description of the interpersonal covariance structure of earnings. There are two types of cross-person relationships that are of interest to our analysis: i) between members of the same family (brothers), and ii) between members of the same youth community (peers). We consider the two most important dimensions of the community; the school attended at age 15 and the neighborhood (parish) of residence at the same age.

The covariance of earnings among brothers is computed from families with at least two male children. We group non-sibling peers in clusters depending on whether they shared the school and the neighborhood, only the school, or only the neighborhood. We obtain the between-peers covariance of earnings (at each relevant age) by first computing the withincluster covariance and then averaging covariances between clusters using the weighting scheme of Page and Solon (2003, pp. 840), which gives more importance to more populated clusters.

We begin by describing the sibling earnings correlation by age in Figure 1. The plot labeled "Same age" reports the computed correlation when the brothers are at the same point in their life cycle, a counterfactual that is available in our data. The earnings correlation declines between age 24 and 30 , and remains stable after age 30 . The decline suggests that sources of initial earnings heterogeneity that are shared between brothers are negatively correlated with heterogeneity in earnings growth. As discussed in Section 2, human capital models predict investments in education or training to induce such a negative correlation. The second plot labeled "Age B1=35" fixes the age of the older among the two brothers at 35 and reports the sibling correlation by age of the younger brother. In this case, the earnings correlation is relatively low at age 24 (actually close to zero) and increases sharply so that by the early-30s it matches the figure labeled "Same age". This pattern illustrates that the earnings correlation computed between siblings of different ages is an underestimate of the correlation one would obtain observing siblings at the same point in the life-cycle. This is a
form of life-cycle bias discussed in Jenkins (1987) and Haider and Solon (2006). The figure shows that we can observe this bias in the data and that we have the information required for controlling it in estimation.

Besides human capital investments, the large contemporaneous associations at the early stage of the lifecycle in Figure 1 may also reflect the correlation of transitory shocks. It is well known that earnings instability is large for young cohorts (see e.g. Baker and Solon, 2003). It is also plausible that siblings are subject to common shocks, for example, because of similar local economic conditions at labor market entry. As a way to assess if the relatively large sibling correlation at young ages is driven by permanent earnings differences or transitory fluctuations, we also computed sibling correlations for brothers born at least five, eight or ten years apart, which are shown in Figure 2. The larger the age difference, the less likely it is that brothers entered the same labor market and shared transitory shocks at entry, so that these samples are less likely to be influenced by transitory fluctuations compared with the samples underlying Figure 1. A declining pattern of the sibling correlation between the mid-20s and the early-30s persists even after excluding closely spaced brothers that most likely share transitory earnings fluctuations. This suggests that the source of the convex evolution of sibling correlations is in the permanent earnings component.

In Figure 3 we plot the earnings correlations for non-relative peers at the same point in their life-cycle distinguishing between those sharing both the school and the neighborhood, sharing only the school, or only the neighborhood. These empirical correlations pick-up all sources of peer similarities, both those correlated with family effects and those independent of them. A few points are worth mentioning in this graph. The first is the magnitude of the peer earnings correlation, which is roughly one tenth of the correlation of sibling earnings reported in Figures 1 and 2. Second, the earnings correlation is higher at the beginning of the life-cycle and up to age 30, which implies that after that age the influence of peers appears to be negligible. Third, schools seem to exhibit stronger influence compared to neighborhoods.

Finally, the graph also reports the correlation of earnings for "Unrelated" peers, i.e. nonrelatives that share neither the school nor the neighborhood. This correlation is computed by randomly matching each individual in the sample with 1000 unrelated peers of the same age. We find this correlation to be equal to zero at each age, which suggests that the evolution of sibling and peer correlations over age is picking up some underlying forces due to families, schools and neighborhoods, and is not simply an artifact of age effects.

## 5. Econometric model

We exploit information on the joint earnings dynamics of brothers, schoolmates and neighbors over the life cycle to develop an earnings model with family, school and neighborhood effects, and use its estimates to decompose the sibling correlation of permanent earnings into these three components. We consider full biological brothers who share both parents. As discussed in detail in Section 3, in the baseline model we define schoolmates as individuals attending the same school at the age of 15 , which corresponds to the end of compulsory education in Denmark. Neighbors are defined as individuals sharing the parish of residence also at age 15. We tackle the estimating challenges highlighted in the literature (transitory shocks and life-cycle biases) with a model of multi-person earnings dynamics distinguishing permanent from transitory earnings and allowing for heterogeneous earnings growth.

The logs of age- and time- adjusted gross annual earnings, denoted by $w$, are assumed to be the sum of two components, a permanent one denoted by $(y)$ and a transitory one denoted by ( $v$ ), which are orthogonal by definition:

$$
\begin{equation*}
w_{i f s n a}=y_{i f s n a}+v_{i f s n a} ; E\left(y_{i f s n a} v_{i f s n a}\right)=0, \tag{1}
\end{equation*}
$$

where the indices $i, f, s, n$ and $a$ stand for individual, family, school, neighborhood and age. ${ }^{7}$ Separate identification of permanent and transitory earnings is granted by the availability of individual level panel data, which ensures that we estimate correlations in permanent earnings, avoiding measurement error biases due to transitory shocks.

### 5.1 Specification of permanent earnings

We allow permanent earnings $(y)$ to depend on both shared and idiosyncratic components. Shared components capture those determinants of permanent earnings that are common between brothers, schoolmates and neighbors. The idiosyncratic component represents individual-specific sources of variation in permanent earnings. We model life cycle dynamics of shared components using a specification based on heterogeneous income profiles (HIP), which is also known as a random growth model. We augment this with a restricted income profile (RIP) process for individual-specific components, which is an idiosyncratic unit root (random walk) shock.

As discussed in Section 2, the heterogeneous income profiles specification is inspired by human capital models in which heterogeneity of initial earnings and heterogeneous earnings growth are generated by differential investments (Mincer, 1958; Ben-Porath, 1967). More specifically, these models predict that heterogeneous investments in human capital induce a negative correlation between initial earnings and earnings growth rates, because investors trade off initial earnings against earnings growth throughout the life cycle. The resulting negative covariance of intercepts and growth rates would generate a u-shaped evolution of earnings dispersion by age due to the 'Mincerian cross-overs' of earnings profiles. Combining these observations with insights from the Becker and Tomes (1979) model of parental preferences for child human capital, motivates our specification choice for shared earnings determinants, reflecting the idea that resemblance of earnings across

[^5]individuals stems from similarities in social background and human capital investments. We showed in Section 4 that life cycle patterns of earnings correlations between siblings and peers are consistent with these mechanisms.

Besides the earnings profile shared by siblings and peers, we assume permanent earnings to follow a unit root in age ( $\omega_{i a}$ ), which captures long-term individual deviations from the shared profile. This represents idiosyncratic ability revealed over time, either to the labor market. or to individuals themselves. Overall, our permanent earnings model is specified as follows:

$$
\begin{gather*}
y_{i f s n a}=\pi_{t}\left[\left(\mu_{f}+\mu_{s}+\mu_{n}\right)+\left(\gamma_{f}+\gamma_{s}+\gamma_{n}\right) a+\omega_{i a}\right]  \tag{2}\\
\omega_{i a}=\omega_{i(a-1)}+\xi_{i t} ; t=c(i)+24+a
\end{gather*}
$$

where $c(i)$ is the birth cohort of person $i$ and $\pi_{t}$ is a calendar time shifter, allowing for the possibility of aggregate changes of the permanent earnings process over time.

The parameters of the individual-specific linear profile of earnings are factored into three zero-mean components. Their variances capture family, school and neighborhood heterogeneity in initial earnings (the $\mu \mathrm{s}$ ) and life-cycle earnings growth (the $\gamma \mathrm{s}$ ). We allow for arbitrary correlation of initial and growth rate heterogeneity within each of the shared components. We also allow for arbitrary correlation across each of the shared components, which is important for taking into account sorting of families across communities (schools and neighborhoods). While previous studies of neighbor and sibling correlations have acknowledged the importance of sorting of family into communities (see Page and Solon, 2003, Oreopoulos, 2003 and Raaum et al., 2006), this is arguably the first attempt to actually estimate these sorting correlations.

The assumptions on the variance-covariance structure of permanent earnings are as follows:

$$
\begin{equation*}
\left(\mu_{f}, \gamma_{f}\right) \sim\left(\sigma_{\mu \Phi}^{2}, \sigma_{\gamma_{\Phi}}^{2}, \sigma_{\mu \gamma \Phi}\right) \tag{3.a}
\end{equation*}
$$

$$
\begin{gather*}
\left(\mu_{s}, \gamma_{s}\right) \sim\left(\sigma_{\mu \Sigma}^{2}, \sigma_{\gamma \Sigma}^{2}, \sigma_{\mu \gamma \Sigma}\right)  \tag{3.b}\\
\left(\mu_{n}, \gamma_{n}\right) \sim\left(\sigma_{\mu \mathrm{N}}^{2}, \sigma_{\gamma \mathrm{N}}^{2}, \sigma_{\mu \gamma \mathrm{N}}\right)  \tag{3.c}\\
\left(\mu_{f}, \mu_{s}, \mu_{n}\right) \sim\left(\sigma_{\mu \Phi \Sigma}, \sigma_{\mu \Phi \mathrm{N}}, \sigma_{\mu \Sigma \mathrm{N}}\right)  \tag{3.d}\\
\left(\omega_{i 24}, \xi_{i a}\right) \sim\left(0,0 ; \sigma_{\omega_{24} b}^{2}, \sigma_{\xi b}^{2}\right), b=1,2 \tag{3.e}
\end{gather*}
$$

where idiosyncratic parameters are allowed to vary by birth order (denoted by $b$ in eq. 3), while capital Greek letters indicate to which dimension of heterogeneity a variancecovariance parameter refers to (family, school, neighborhood, or their combination). Correlation across family and community effects is allowed through the intercepts of the individual-specific profiles (assumption (3.d)), both because empirically most of the community effects vanish after two or three years (see Figure 4), and not to overcrowd the parameter space.

### 5.2 Specification of transitory earnings

We model transitory earnings ( $v$ ) using an autoregressive $\mathrm{AR}(1)$ process in order to capture any serial correlation of transitory shocks. We allow brothers to draw shocks from birth order specific distributions and we account for age effects in the variance of these shocks through an exponential spline. Our model for transitory earnings can be summarized as follows:

$$
\begin{align*}
& v_{i f s n a}=\eta_{t} u_{i f s n a} ; u_{i f s n a}=\rho_{b} u_{i f s n(a-1)}+\varepsilon_{i f s n a} ; \\
& \quad \varepsilon_{i f s n a} \sim\left(0, \sigma_{\varepsilon b}^{2} \exp \left(g_{b}(a)\right)\right), u_{i f s n 24} \sim\left(0, \sigma_{u_{24} b}^{2}\right), \tag{4}
\end{align*}
$$

where $\eta_{t}$ is a time loading factor, and $u_{i f s n a}$ is the birth order specific $\operatorname{AR}(1)$ process (note the index $b$ ). The autoregressive process begins at age 24 and we specify the variance of the initial condition $\left(\sigma_{u_{24} b}^{2}\right)$. The process evolves through the arrival of white noise shocks (denoted by $\varepsilon$ ) whose variance is age-specific $\left(\sigma_{\varepsilon b}^{2} \exp \left(g_{b}(a)\right)\right.$, with $g_{b}(a)$ denoting a linear spline in age with knots at $28,33,38$ and 43 ).

We allow transitory earnings to be correlated across individuals. The specific way in which we model such correlation depends on the type of relationship between individuals. For brothers, the use of birth order specific distributions of shocks enables us to identify the contemporaneous correlation of $\operatorname{AR}(1)$ innovations. Let $i$ and $i^{\prime}$ index two individuals; the brother correlation of $\operatorname{AR}(1)$ innovation is as specified as follows:

$$
\begin{equation*}
E\left(\varepsilon_{i f s n a} \varepsilon_{i^{\prime} f s^{\prime} n^{\prime} a^{\prime}}\right)=\sigma_{f}, \quad \forall s, s^{\prime}, n, n^{\prime}, a=a^{\prime} \pm\left|c(i)-c\left(i^{\prime}\right)\right| . \tag{5}
\end{equation*}
$$

That is, when the individuals belong to the same family and when their age difference is such that the two shocks belong to the same time period, these shocks are allowed to be correlated with covariance denoted by $\sigma_{f}$. This correlation of shocks between siblings does not depend on whether the two brothers attended the same school, or lived in the same parish when they were aged 15 and is transmitted to non-contemporaneous innovations through the autoregressive structure of the model.

Due to dimensionality issues, we cannot follow a similar approach for modeling the correlation of shocks across community members belonging to different families ( $f$ and $f^{\prime}$ ). Instead, we allow for catch-all "mass-points" covariances ( $\lambda$ ) collapsing all the parameters of the underlying stochastic processes, and allow such covariances to fade away over time. For any two non-necessarily different age levels $a$ and $a^{\prime}$, correlations of transitory shock across non-sibling peers are specified as follows:

$$
\begin{gather*}
E\left(u_{i f s n a} u_{i^{\prime} f^{\prime} s n a^{\prime}}\right)=\lambda_{s n}^{1+\left|t-t^{\prime}\right|}, E\left(u_{i f s n a} u_{i^{\prime} f^{\prime} s n^{\prime} a^{\prime}}\right)=\lambda_{s}^{1+\left|t-t^{\prime}\right|} \forall n \neq n^{\prime},  \tag{6}\\
E\left(u_{i f s n a} u_{i^{\prime} f^{\prime} s^{\prime} n a^{\prime}}\right)=\lambda_{n}^{1+\left|t-t^{\prime}\right|} \forall s \neq s^{\prime} .
\end{gather*}
$$

### 5.3 Identification of permanent earnings components and decomposition of the sibling

## correlation

Assumptions (3.a) - (3.e) fully specify the intertemporal and interpersonal distribution of permanent earnings. ${ }^{8}$ Identification of parameters is achieved by exploiting different types of moment restrictions generated by the model. For a given individual, moment restrictions for two time periods are a function of all sources of earnings heterogeneity, which include the idiosyncratic component, as well as the components due to the influences from the family, the school and the neighborhood. The moment restrictions for a single individual for two nonnecessarily different age levels $a$ and $a^{\prime}$ can be written as follows:

$$
\begin{align*}
& E\left(y_{i f s n a}, y_{i f s n a^{\prime}}\right)=  \tag{7}\\
& \left\{\sigma_{\mu \Phi}^{2}+\sigma_{\mu \Sigma}^{2}+\sigma_{\mu \mathrm{N}}^{2}+\left(\sigma_{\gamma \Phi}^{2}+\sigma_{\gamma \Sigma}^{2}+\sigma_{\gamma \mathrm{N}}^{2}\right) a a^{\prime}+\left(\sigma_{\mu \gamma \Phi}+\sigma_{\mu \gamma \Sigma}+\sigma_{\mu \gamma \mathrm{N}}\right)\left(a+a^{\prime}\right)+2 \sigma_{\mu \Phi \Sigma}\right. \\
& \left.+2 \sigma_{\mu \Phi \mathrm{N}}+2 \sigma_{\mu \Sigma \mathrm{N}}+\sigma_{\omega_{24} b}^{2}+\sigma_{\xi b}^{2} \min \left(a, a^{\prime}\right)\right\} \pi_{t} \pi_{t^{\prime}}
\end{align*}
$$

Cross-persons moments (across siblings, neighbors, or schoolmates) do not depend on idiosyncratic heterogeneity. Moment restrictions between siblings (different $i$ but same $f$ ) depend on the family effects. Moreover, they are also functions of school effects, neighborhood effects, both, or none, depending on the extent to which siblings shared schools and/or neighborhoods. ${ }^{9}$ Moment restrictions for siblings can be written as follows:

$$
\begin{align*}
E\left(y_{i f s n a}, y_{i^{\prime} f s^{\prime} n^{\prime} a^{\prime}}\right)= & \left\{\sigma_{\mu \Phi}^{2}+\sigma_{\gamma \Phi}^{2} a a^{\prime}+\sigma_{\mu \gamma \Phi}\left(a+a^{\prime}\right)+I\left(s=s^{\prime}\right)\left[\sigma_{\mu \Sigma}^{2}+\sigma_{\gamma \Sigma}^{2} a a^{\prime}+\right.\right.  \tag{8}\\
& \left.\sigma_{\mu \gamma \Sigma}\left(a+a^{\prime}\right)\right]+I\left(n=n^{\prime}\right)\left[\sigma_{\mu \mathrm{N}}^{2}+\sigma_{\gamma \mathrm{N}}^{2} a a^{\prime}+\sigma_{\mu \gamma \mathrm{N}}\left(a+a^{\prime}\right)\right]+ \\
& \left.2 \sigma_{\mu \Phi \Sigma}+2 \sigma_{\mu \Phi \mathrm{N}}+2 \sigma_{\mu \Sigma \mathrm{N}}\right\} \pi_{t} \pi_{t^{\prime}},
\end{align*}
$$

where $I(\quad)$ is an indicator function. Equation (8) nests moments restrictions for four types of siblings, corresponding to the four elements of the set generated by intersecting $I\left(s=s^{\prime}\right)$ and $I\left(n=n^{\prime}\right)$. These types include siblings who: (1) share both the school and the neighborhood;

[^6](2) share only the school; (3) share only the neighborhood; and (4) share only the family but neither the school nor the neighborhood.

The above moment conditions are sufficient for identifying family, school, and neighborhood effects, because school and neighborhood effects are identified by the presence of siblings that went to different schools or grew up in different neighborhoods due to family mobility. However, the cross-effects covariances are not identified. This is evident from the fact that the term $2 \sigma_{\mu \Phi \Sigma}+2 \sigma_{\mu \Phi \mathrm{N}}+2 \sigma_{\mu \Sigma \mathrm{N}}$ enters equation (8) irrespective of whether siblings went to the same school or lived in the same parish. Because families sort across schools and neighborhoods, school and neighborhood effects are always correlated between brothers, and such covariance is not separable from the variance of family effects $\sigma_{\mu \Phi}^{2}$. To identify the sorting parameters $\sigma_{\mu \Phi \Sigma}, \sigma_{\mu \Phi \mathrm{N}}$ and $\sigma_{\mu \Sigma \mathrm{N}}$, we exploit moment restrictions for non-sibling peers that do not share the family effect. Using these restrictions is also helpful for estimating community effects without relying exclusively on family mobility across communities. Moment restrictions for peers belonging to different families $f$ and $f^{\prime}$ can be written as follows:

$$
\begin{align*}
E\left(y_{i f s n a}, y_{i^{\prime} f^{\prime} s^{\prime} n^{\prime} a^{\prime}}\right)= & \left\{I\left(s=s^{\prime}\right)\left[\sigma_{\mu \Sigma}^{2}+\sigma_{\gamma \Sigma}^{2} a a^{\prime}+\sigma_{\mu \gamma \Sigma}\left(a+a^{\prime}\right)+2 \sigma_{\mu \Phi \Sigma}\right]+\right.  \tag{9}\\
& I\left(n=n^{\prime}\right)\left[\sigma_{\mu \mathrm{N}}^{2}+\sigma_{\gamma \mathrm{N}}^{2} a a^{\prime}+\sigma_{\mu \gamma \mathrm{N}}\left(a+a^{\prime}\right)+2 \sigma_{\mu \Phi \mathrm{N}}\right]+ \\
& \left.2 \sigma_{\mu \Sigma \mathrm{N}}\right\} \pi_{t} \pi_{t^{\prime}}
\end{align*}
$$

Equation (9) nests moment restrictions for three types of peers depending on them sharing the school, the neighborhood or both. This identifies the three sorting parameters, where the covariance is zero for those who do not share any community effect. Note that the covariance between family and a given community effect (school or neighborhood) enters the moment restrictions in (8) only for peers sharing that specific effect.

Using parameter estimates from the model we can predict the contributions of each factor to the sibling correlation of permanent earnings over the life cycle as follows:

$$
\begin{equation*}
r^{F}(a)=\frac{E\left(y_{i f s n a,} y_{i^{\prime} f s^{\prime} n^{\prime} a}\right)}{E\left(y_{i f s n a} y_{i f s n a}\right)}, r^{S}(a)=\frac{E\left(y_{i f s n a,} y_{i^{\prime} f^{\prime} s^{\prime} a}\right)}{E\left(y_{i f s n a} y_{i f s n a}\right)}, r^{N}(a)=\frac{E\left(y_{i f s n a} y_{i^{\prime} f^{\prime} s^{\prime} n a}\right)}{E\left(y_{i f s n a} y_{i f s n a}\right)}, \tag{10}
\end{equation*}
$$

where $r$ denotes correlation coefficients of permanent earnings, $F, S$ and $N$ denote the three relevant dimensions of heterogeneity (family, school, neighborhood). It should be emphasized that correlations vary with age because they are estimated from a model of life cycle earnings. Given the model assumptions, the sibling correlation of permanent earnings is the sum of the three components:

$$
\begin{equation*}
r^{B}(a)=r^{F}(a)+r^{S}(a)+r^{N}(a) \tag{11}
\end{equation*}
$$

### 5.4 Estimation

The model is estimated by Minimum Distance which matches moment restrictions implied by the model to the empirical moments derived from the data. ${ }^{10}$ Empirical moments are based on the residuals after regressing log real gross annual earnings on time dummies and a quadratic age trend by birth cohort. There are three types of empirical moments entering into the estimation. First, there are individual moments which include the variances and inter-temporal covariances of individual earnings. Second there are sibling moments which are defined only in families where there are at least two brothers. This implies that each family contributes at most one observation in the estimation of sibling empirical moments, where families with only one son do not contribute to such estimation. ${ }^{11}$ We estimate separate empirical moments for siblings depending on whether they shared the school, the neighborhood, both or none, so as to match the four different moment restrictions that are nested in equation (8). Finally, there are empirical moments for non-sibling peers who shared the community. Differently from the case of families, the numerosity of peers within community clusters do vary. We

[^7]account for such varying importance of community clusters using the weighting scheme proposed by Page and Solon (2003, pp. 841). In particular, we first estimate the within-cluster covariances and then we take the between-clusters weighted average of within-cluster covariances using weights that are proportional to the number of individuals in that cluster. Similar to the case for siblings, we estimate empirical moments distinguishing whether peers shared the school, the neighborhood, or both.

## 6. Results

We concentrate our discussion of the results on estimates of the 'core' parameters of the permanent and transitory components. ${ }^{12}$ We present the results for the parameter estimates of the permanent component in Section 6.1 and those for the transitory component in Section 6.2. Sensitivity analysis and heterogeneous effects are discussed in Sections 6.3 and 6.4, respectively.

### 6.1 Permanent earnings correlation between siblings, schoolmates and neighbors

Based on equation (2) permanent earnings depend on both shared and idiosyncratic components. The parameters estimates of the shared components indicate that the family is by far the most relevant factor that shapes long-term earnings (Table 2, Panel A). This is true both for initial earnings and for earnings growth rates. In particular, there is no statistically significant heterogeneity in initial earnings related to school and neighborhood effects on top of the sorting effects captured by the covariances between family and community components (see the discussion below). The other relevant source of permanent inequality in earnings is the individual idiosyncratic component (Table 2, Panel B).

All shared components of long-term earnings in Table 2 display the Mincerian crossover property. This is apparent by noting that all covariances between intercepts and slopes of

[^8]earnings profiles are negative. This indicates that families associated with low earnings at age 24 are also associated with faster growth in life-cycle earnings. This implies that the variance of permanent earnings across families is $u$-shaped in age because it falls in the years of catch up and increases after the cross over point. The point of cross over can be computed as the year in which the earnings variance is minimized, and it is located at age 34 for the betweenfamilies earnings distribution. A similar u-shape pattern of the variance of earnings over age is also observed across schools and across neighborhoods. The cross over point is age 36 for the between-neighbors earnings distribution, and age 38 for the between-schools earnings distribution.

Panel A of Table 2 also reports estimates of the covariances across the three components of shared earnings determinants, which capture the sorting of families into communities (schools and neighborhoods). ${ }^{13}$ Our results indicate that these sorting effects are relevant, as the covariance of family effects with both school and neighborhood effects is positive, sizeable and statistically significant. These effects imply that a high draw from the distribution of family effects in permanent earnings is associated with similarly high draws in the distributions of school and neighborhood effects. We also find a positive covariance among community effects, which suggests that school and neighborhood effects are positively correlated.

We use these parameter estimates to generate predictions, based on the formulae provided in Section 5.3, of the sibling correlation and its decomposition into the three factors of interest: family, school and neighborhood. In particular, we consider the case of two brothers who attended the same school and lived in the same neighborhood when they were 15 , so that the resulting sibling correlation is the sum of family, school and neighborhood effects. As shown in Figure 4, the life-cycle pattern of the sibling correlation is u-shaped in

[^9]age. More specifically, the estimated correlation is about 0.6 at age 24 , drops to 0.15 at age 37, and rises back to 0.34 by age 51, which is the last age we observe younger brothers. The average sibling correlation is 0.28 (s.e. 0.012 ), which is in line with previous estimates for Denmark. ${ }^{14}$ As we discussed earlier, the u-shaped pattern is a symptom of "Mincerian crossovers" of earnings profiles. That is, the negative estimates of the covariance between intercept and slopes for all the shared factors of earnings profiles imply that the distribution of shared components, and therefore the sibling and peer correlations, first shrink and then fan out over the life cycle. The same u-shaped pattern was also a feature of the raw cross-person covariances in Figures 1 to 3, and in particular Figure 2, which depicted siblings’ earnings covariances for brothers with few years of age spacing.

Considering the decomposition of the sibling correlation in Figure 2, it is evident that family accounts for most of the dispersion of permanent earnings over the life-cycle. The community effects are very small and are only significant at the beginning of the life cycle, while by age 30 they become negligible and not significantly different from zero. On average, over the life-cycle, we estimate the correlation in permanent earnings across schoolmates to be 0.004 (s.e. 0.010 ), and across neighbors to be 0.009 (s.e. 0.010 ). These results indicate that the only factor that generates a substantial correlation in permanent earnings between brothers is the family. Instead, there is not much room for community effects in shaping the sibling correlation.

Our findings are in line with those of Oreopoulos (2003) who used quasi-random assignment of neighbors and showed that the neighbors correlation in adult earnings was virtually zero in a variance decomposition exercise similar in spirit to ours. Page and Solon (2003), instead, found in the PSID that the neighbors correlation was about half of the sibling correlation ( 0.16 versus 0.34 ). By formulating a model for the joint estimation of family and

[^10]community effects, allowing for sorting of families into communities, we can replicate the previous approaches by estimating community effects on a sample that excludes siblings and constraining family-related model parameters to be zero. The idea of this exercise is that, by ignoring family effects and their sorting into communities, community effects would capture not only the effects of communities but will also pick up the influence of families. The results of this exercise are reported in Figure 5 in which we plot community effects (the sum of school and neighborhood effects) from the model that ignores family effects, alongside community effects estimated from our full model. The comparison is striking. When we ignore the family we find a sizeable correlation among members of the youth community, which is significant throughout the life-cycle. The average correlation in this model is 0.071 (s.e. 0.001 ), which amounts at $25 \%$ of the sibling correlation. ${ }^{15}$ As we have seen in Figure 4, the model that controls for family effects tells a radically different story about the relevance of community effects, with a correlation of permanent earnings between members of the same youth community of just 0.013 (s.e. 0.009 ), which is a factor of 5 smaller than the model that ignores family effects and insignificant. The comparison depicted in Figure 5 suggests that including family effects in the model of life-cycle earnings allows controlling for the sorting of families into neighborhoods with results that are close to those from quasi-randomized variation of families across communities that aim to control for that type of selection.

### 6.2 Transitory earnings

Parameter estimates of transitory earnings in Table 3 show a clear age pattern of transitory shocks, whose variance decreases between the mid-20s and the mid-30s, while the decrease slows down after age 35 . The sharp decline followed by a leveling-off is consistent with the patterns reported by Baker and Solon (2003) who find the variance of transitory shocks to be declining at decreasing rates between the ages of 25 and 45. These patterns look similar

[^11]between brothers. Also, the autoregressive coefficient (roughly 0.5 ) is very similar between brothers and of a moderate size. Table 3 shows that transitory shocks are contemporaneously correlated between brothers. However, compared to the variance of the shocks, the size of the covariance is negligible. The model also yields estimates of the covariance in transitory earnings between non-relative peers, which turn out to be negligible and imprecisely estimated.

### 6.3 Sensitivity analysis

We subject our results to several sensitivity checks by estimating the model for different family sizes (up to 2 or up to 3 children), excluding singletons, and by varying the degree of exposure to communities. We report in Table 4 the average sibling correlation and its decomposition by family, school and neighborhood factors. Overall, the findings from these additional estimations do not change the main conclusion from the baseline model that family accounts for most of the variation in permanent earnings, while the influence of the community factors is negligible.

With regard to the definition of youth communities one concern is that the definition in the baseline model is based on membership only at age 15, which might miss part of the effects of communities due to potentially limited exposure (see also Gibbons et al., 2013; Chetty et al. 2015 for similar discussions). To address this concern, we re-estimated the model using two alternative criteria to define community membership, which are characterized by greater exposure to communities relative to the one-year definition used in the baseline model. First, we define school mates and neighbors as individual sharing schools and neighborhoods, respectively, for two years during both ages 14 and 15. Second, we define the
neighborhood as the prevalent parish of residence between ages 14 and $18 .{ }^{16}$ As reported in Table 4, none of these alternative definitions alters our finding that community effects account for only a limited share of the sibling correlation in earnings. Defining peers as those sharing schools and neighborhoods both at age 14 and 15, yields an average correlation of permanent earnings between schoolmates equal to 0.002 (s.e. 0.009), and an average correlation between neighbors equal to 0.010 (s.e. 0.010 ). Similarly, when we use the parish in which individuals lived most frequently between the ages of 14 and 18 as identifier of youth neighborhoods we find the average earnings correlation among neighbors to be 0.008 (s.e. 0.010), and the correlation among schoolmates to be 0.006 (s.e. 0.009 ). Based on this evidence it seems plausible to conclude that our finding of negligible community effect is not driven by the specific community definition that we adopt. However, due to data limitations we are not able to consider school and neighborhood effects at earlier age than 14 , so we cannot test whether the effect of exposure at a younger age might differ.

### 6.4 Heterogeneous effects

We now turn to potential heterogeneity by the type of family, school or neighborhood. For families, we distinguish between high and low educated father; for schools, between large and small classes; and for neighborhoods between high and low density areas (urban vs. rural).

Starting with family heterogeneity, Figure 6 shows that the share of the variation in permanent earnings accounted for by the family is much higher among families with a high educated father compared to a low educated father. This is not surprising as families with higher education are more likely to transmit resources to their children which influence their earnings capacity.

[^12]With regard to school heterogeneity, we split observations depending upon whether school enrollment in the grade attended at age 15 was above or below the threshold of 24 pupils used in Denmark for splitting classes. Individuals who attended schools at age 15 with total enrollment below 24, between 37 and 48, between 61 and 72, and so on, were grouped in the "Large Class" group. On the other hand, individuals who attended schools at age 15 with enrollment between 25 and 36, between 49 and 60 and so on, were grouped in the "Small Class" sample. That is because larger cohorts exceeding the class size threshold were split into smaller classes. Figure 6 shows that the school effect is much higher for small classes compared to large classes. This finding is consistent with the literature on the effect of class size on earnings, which suggests a positive effect from smaller classes (e.g. Chetty et al. 2011, Fredriksson et al. 2013). However, the school effect is not persistent and becomes insignificant after age 30. This suggests that although schools resources seem to play a larger role at the beginning of the working life, these effects do not seem to be very long-term effects.

The last dimension of heterogeneity that we take into account is urbanicity by exploiting information on population density (measured in 1976) in the parishes individuals lived in when they were 15 . Specifically, we cut the density distribution across parishes at the upper third, and consider urban individuals living in parishes that are above this threshold, and rural all remaining individuals. Figure 6 shows very similar patterns for both subsamples with negligible and insignificant community effects.

## 7. Conclusion

This paper develops a unified framework which enables disentangling the contribution of families, schools and neighborhoods in labor earnings over the life-cycle. This is achieved within a model of multi-person earnings dynamics distinguishing permanent from transitory earnings and allowing for heterogeneous earnings growth. The analysis is based on
administrative registers from the Danish population which we use to link brothers, schoolmates and teenage neighbors and follow them over their life-cycle and up to age 51.

Our analysis indicates that family is by far the most relevant factor that shapes longterm earnings. The contribution coming from schools and neighborhoods on long-term earnings is overestimated if the family component is ignored, which suggests that not taking sorting into account leads to an upward bias in the estimated influence of community background. Despite the negligible average community effects, we find that both schools and neighborhoods exhibit a positive and significant effect at the beginning of working life. However, these effects are not long-lasting as by age 30 they become close to zero and insignificant. These results contribute to our understanding about the effects of family and community background on labor market outcomes showing that while family influences are long-term, community influences do not have very long-term consequences lasting beyond age 30. This has implications for the design of policies aiming at reducing inequalities in the long-run suggesting that resources aimed at improving the situation of families are likely to be more effective in the very long-term than resources devoted to transforming communities.

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Table 1
Cohorts included in the sample

| Birth Year | First Year Observed | Number of Years Observed | Last Age Observed |
| :---: | :---: | :---: | :---: |
| $1960-61$ | 1984 | 28 | 51 |
| $1962-63$ | 1986 | 26 | 49 |
| $1964-65$ | 1988 | 24 | 47 |
| $1966-67$ | 1990 | 22 | 45 |
| $1968-69$ | 1992 | 20 | 43 |
| $1970-71$ | 1994 | 18 | 41 |
| $1972-73$ | 1996 | 16 | 39 |
| $1974-75$ | 1998 | 14 | 37 |
| $1976-77$ | 2000 | 12 | 35 |
| $1978-79$ | 2002 | 10 | 33 |
| $1980-81$ | 2004 | 8 | 31 |
| $1982-83$ | 2006 | 6 | 29 |

## Table 2

## Parameter estimates of permanent earnings

Panel A - Shared components (heterogeneous income profile -random growth)
Coef. s.e.

Variance of intercepts

| Variance of intercepts |  |  |
| :--- | :---: | :---: |
| Family $\left(\sigma_{\mu \Phi}^{2}\right)$ | 0.0633 | 0.0109 |
| School $\left(\sigma_{\mu \Sigma}^{2}\right)$ | 0.0022 | 0.0031 |
| Neighbor $\left(\sigma_{\mu \mathrm{N}}^{2}\right)$ | 0.0034 | 0.0035 |
|  |  |  |
| Family $\left(\sigma_{\gamma \Phi}^{2}\right)$ | 0.0003 | 0.00006 |
| School $\left(\sigma_{\gamma \Sigma}^{2}\right)$ | 0.00003 | 0.00002 |
| Neighbor $\left(\sigma_{\gamma \mathrm{N}}^{2}\right)$ | 0.0001 | 0.00002 |

Covariance intercepts-slopes

| Family $\left(\sigma_{\mu \gamma \Phi}\right)$ | -0.0039 | 0.0006 |
| :--- | :--- | :--- |
| School $\left(\sigma_{\mu \gamma \Sigma}\right)$ | -0.0005 | 0.0002 |
| Neighbor $\left(\sigma_{\mu \gamma \mathrm{N}}\right)$ | -0.0010 | 0.0003 |

Covariance between components

| Family-School $\left(\sigma_{\mu \Phi \Sigma}\right)$ | 0.0037 | 0.0012 |
| :--- | :--- | :--- |
| Family-Neighbor $\left(\sigma_{\mu \Phi \mathrm{N}}\right)$ | 0.0037 | 0.0013 |
| School- Neighbor $\left(\sigma_{\mu \Sigma \mathrm{N}}\right)$ | 0.0011 | 0.0002 |

Panel B - Idiosyncratic components (restricted income profile-random growth)
$\longrightarrow$ Coef. s.e.

Initial condition (age 24)

| Brother $1\left(\sigma_{\omega 24,1}^{2}\right)$ | 0.0542 | 0.0091 |
| :--- | :--- | :--- |
| Brother2 $\left(\sigma_{\omega 24,2}^{2}\right)$ | 0.0374 | 0.0067 |

Variance of innovations

| Brother $1\left(\sigma_{\xi 1}^{2}\right)$ | 0.0066 | 0.0011 |
| :--- | :--- | :--- |
| Brother $2\left(\sigma_{\xi 2}^{2}\right)$ | 0.0071 | 0.0012 |

## Table 3

## Parameter estimates of transitory earnings

Coef.
s.e.

Initial condition (age 24)

| Brother $1\left(\sigma_{24,1}^{2}\right)$ | 0.6613 | 0.0447 |
| :--- | :--- | :--- |
| Brother $2\left(\sigma_{24,2}^{2}\right)$ | 0.6477 | 0.0459 |

Variance of innovations at 25

| Brother $1\left(\sigma_{\varepsilon 1}^{2}\right)$ | 0.4935 | 0.0357 |
| :--- | :---: | :--- |
|  |  |  |
| Brother $2\left(\sigma_{\varepsilon 2}^{2}\right)$ | 0.4731 | 0.0341 |

Age splines in variance of innovations
Brother 1
26-28

| -0.1370 | 0.0083 |
| :--- | :--- |
| -0.1016 | 0.0058 |
| -0.0244 | 0.0076 |
| -0.0358 | 0.0100 |
| -0.0153 | 0.0110 |

Brother 2
26-28

| -0.1515 | 0.0089 |
| :--- | :--- |
| -0.1122 | 0.0066 |
| -0.0364 | 0.0092 |
| -0.0184 | 0.0125 |
| 0.0080 | 0.0175 |

Autoregressive coefficient

| Brother $1\left(\rho_{1}\right)$ | 0.4979 | 0.0049 |
| :--- | :--- | :--- |
| Brother $2\left(\rho_{2}\right)$ | 0.5164 | 0.0053 |

Cross-person associations in transitory earnings

| Sibling covariance of innovations $\left(\sigma_{f}\right)$ | 0.0072 | 0.0006 |
| :--- | :--- | :--- |

Peers covariance of transitory earnings (catchall components)

| Sharing both school and neighbor $\left(\lambda_{s n}\right)$ | -0.0003 | 0.0006 |
| :--- | :---: | :---: |
| Sharing only school $\left(\lambda_{s}\right)$ | 0.0027 | 0.0007 |
| Sharing only neighbor $\left(\lambda_{n}\right)$ | -0.0006 | 0.0007 |

Table 4
Sensitivity analysis - Decomposition of sibling correlation (Average)

|  | Sibling | Family | Neighborhood | School | Community ( $\mathrm{N}+\mathrm{S}$ ) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Baseline | $\begin{gathered} 0.282 \\ (0.012) \end{gathered}$ | $\begin{gathered} 0.269 \\ (0.012) \end{gathered}$ | $\begin{gathered} 0.009 \\ (0.010) \end{gathered}$ | $\begin{gathered} \hline 0.004 \\ (0.010) \end{gathered}$ | $\begin{gathered} 0.013 \\ (0.009) \end{gathered}$ |
| Families with up to 2 Children | $\begin{gathered} 0.329 \\ (0.016) \end{gathered}$ | $\begin{gathered} 0.311 \\ (0.022) \end{gathered}$ | $\begin{gathered} 0.021 \\ (0.014) \end{gathered}$ | $\begin{aligned} & -0.004 \\ & (0.013) \end{aligned}$ | $\begin{gathered} 0.018 \\ (0.013) \end{gathered}$ |
| Families with up to 3 Children | $\begin{gathered} 0.293 \\ (0.014) \end{gathered}$ | $\begin{gathered} 0.292 \\ (0.018) \end{gathered}$ | $\begin{gathered} 0.020 \\ (0.015) \end{gathered}$ | $\begin{aligned} & -0.019 \\ & (0.013) \end{aligned}$ | $\begin{gathered} 0.001 \\ (0.012) \end{gathered}$ |
| No singleton | $\begin{gathered} 0.286 \\ (0.012) \end{gathered}$ | $\begin{gathered} 0.275 \\ (0.012) \end{gathered}$ | $\begin{gathered} 0.008 \\ (0.009) \end{gathered}$ | $\begin{gathered} 0.003 \\ (0.009) \end{gathered}$ | $\begin{gathered} 0.011 \\ (0.009) \end{gathered}$ |
| Peers at age 14 and age 15 | $\begin{gathered} 0.282 \\ (0.012) \end{gathered}$ | $\begin{gathered} 0.270 \\ (0.012) \end{gathered}$ | $\begin{gathered} 0.010 \\ (0.010) \end{gathered}$ | $\begin{gathered} 0.002 \\ (0.009) \end{gathered}$ | $\begin{gathered} 0.012 \\ (0.009) \end{gathered}$ |
| Main parish of residence (age 14-18) | $\begin{gathered} 0.280 \\ (0.012) \\ \hline \end{gathered}$ | $\begin{gathered} 0.267 \\ (0.012) \\ \hline \end{gathered}$ | $\begin{gathered} 0.008 \\ (0.010) \\ \hline \end{gathered}$ | $\begin{gathered} 0.006 \\ (0.009) \\ \hline \end{gathered}$ | $\begin{gathered} 0.014 \\ (0.009) \\ \hline \end{gathered}$ |

Figure 1
Sibling correlation of annual earnings


Figure 2
Sibling correlation of annual earnings by siblings age gap


Figure 3
Correlation of annual earnings for members of youth communities


Figure 4
Predicted sibling correlation of permanent earnings and factor decomposition


Figure 5
Predicted correlations of permanent earnings between members of youth communities Comparison of models with and without family effects


## Figure 6

Predicted correlations of permanent earnings by family, school and neighborhood heterogeneity

Father Low Edu


Small Class


Father High Edu


Rural


Large Class


Urban

$\square$ Sibling + Family $\_$School $\longrightarrow$ Neighbour $\square$ 95\% C.I.

## Appendix A

## Moment restrictions for transitory earnings

Considering two non-necessarily different age levels $a$ and $a^{\prime}$, the intertemporal covariance structure of the transitory component of individual earnings from the birth order specific $\operatorname{AR}(1)$ process is as follows:

$$
\begin{align*}
& \quad E\left(v_{i f s n a} v_{i f s n a^{\prime}}\right)=\left[I\left(a=a^{\prime}=24\right) \sigma_{24 b}^{2}\right. \\
& +I\left(a=a^{\prime}>24\right)\left(\exp \left(g_{b}(a)\right)+\operatorname{var}\left(u_{i f s n(a-1)}\right) \rho_{b}^{2}\right)  \tag{A.1}\\
& \left.+I\left(a \neq a^{\prime}\right)\left(E\left(u_{i f s n(a-1)} u_{i f s n a^{\prime}}\right) \rho_{b}\right)\right] \eta_{t} \eta_{t^{\prime}} .
\end{align*}
$$

Allowing for correlation of $\operatorname{AR}(1)$ innovations across brothers, the model yields restrictions on transitory earnings also for cross-brothers moments:

$$
\begin{gather*}
E\left(v_{i f s n a} v_{i^{\prime} f s^{\prime} n^{\prime} a^{\prime}}\right)= \\
\sigma_{f}\left(\frac{\left(1-\left(\rho_{1} \rho_{2}^{\left|t-t^{\prime}\right|}\right)^{P}\right)}{1-\rho_{1} \rho_{2}^{\left|t-t^{\prime}\right|}}\right)^{I\left(t \leq t^{\prime}\right)}\left(\frac{\left(1-\left(\rho_{2} \rho_{1}^{\left|t-t^{\prime}\right|}\right)^{P}\right)}{1-\rho_{2} \rho_{1}^{\left|t-t^{\prime}\right|}}\right)^{I\left(t>t^{\prime}\right)}  \tag{A.2}\\
\eta_{t} \eta_{t^{\prime}} ; \forall s, s^{\prime}, n, n^{\prime},
\end{gather*}
$$

where $P$ is the number of overlapping years the two brothers are observed in the data.

We also model the correlation of transitory earnings across non-sibling peers. Differently from the case of brothers, we do not model the correlation of $\operatorname{AR}(1)$ innovations among peers because it would require distinguishing idiosyncratic components of transitory earnings for each member of school or neighborhood clusters, generating dimensionality issues. We, therefore, collapse all the cross-peers covariance structure of the transitory component into catch-all "mass point" factors absorbing all the parameters of the underlying stochastic process. For any two non-necessarily different age levels $a$ and $a^{\prime}$, correlations of transitory earnings across non-sibling peers are as follows:

$$
\begin{gather*}
E\left(v_{i f s n a}, v_{i^{\prime} f^{\prime} s n a^{\prime}}\right)=\lambda_{s n}^{1+\left|t-t^{\prime}\right|} \eta_{t} \eta_{t^{\prime}}  \tag{A.13}\\
E\left(v_{i f s n a}, v_{i^{\prime} f^{\prime} s n^{\prime} a^{\prime}}\right)=\lambda_{s}^{1+\left|t-t^{\prime}\right|} \eta_{t} \eta_{t^{\prime}} \forall n \neq n^{\prime} \\
E\left(v_{i f s n a}, v_{i^{\prime} f^{\prime} s^{\prime} n a^{\prime}}\right)=\lambda_{n}^{1+\left|t-t^{\prime}\right|} \eta_{t} \eta_{t^{\prime}} \quad \forall s \neq s^{\prime}
\end{gather*}
$$

The moment restrictions above characterize the inter-temporal distribution of transitory earnings for each individual and between siblings and peers. The orthogonality assumption between permanent and transitory earnings in equation (1) implies that moment restrictions of the full model are the sum of moment restrictions for permanent and transitory earnings, the former being discussed in Section 5.3 of the paper. In general, these restrictions are a nonlinear function of a parameter vector $\theta$. We estimate $\theta$ by Minimum Distance (see Chamberlain, 1984; Haider, 2001). We use Equally Weighted Minimum Distance (EWMD) and a robust variance estimator $\operatorname{Var}(\theta)=\left(G^{\prime} G\right)^{-1} G^{\prime} \operatorname{VG}\left(G^{\prime} G\right)^{-1}$, where $V$ is the fourth moments matrix and $G$ is the gradient matrix evaluated at the solution of the minimization problem.


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[^1]:    ${ }^{1}$ The model extends the joint earnings dynamics model of Bingley and Cappellari (2013) for three persons to a multi-person setting.

[^2]:    ${ }^{2}$ Studies focusing on educational achievement outside the sibling correlation framework but using quasiexperimental variation of neighborhood quality have also found no impact of neighborhoods (e.g. Jacob, 2004; Gibbons et al., 2013).

[^3]:    ${ }^{3}$ Subsequent sons beyond the first two are very few (4 percent) and are not considered in the analysis. The son birth order is determined irrespecitve of daugthers present in the family. We also exclude from the sample sons who were adopted before age 17; sons who are themselves observed as fathers; brothers born less than 12 months apart; and second sons if they are born more than 12 years after the first.
    ${ }^{4}$ Early or late school start and grade retention were uncommon (less than 10 percent), meaning most pupils begin the final year of compulsory schooling in the calendar year they turn fifteen.
    ${ }^{5}$ We exclude special schools from our estimation sample.

[^4]:    ${ }^{6}$ In robustness checks we consider 8th grade attachment or both 8th and 9th grade attachment definitions of schoolmates.

[^5]:    ${ }^{7}$ Age is measured in deviation from the life cycle starting point, which is set at 24 .

[^6]:    ${ }^{8}$ Parameter identification of transitory earnings is discussed in the Appendix.
    ${ }^{9}$ This is one difference with PSID-based studies (e.g. Page and Solon, 2003) in which all siblings share the neighborhood by sampling design.

[^7]:    ${ }^{10}$ Moment restrictions for transitory earnings are given in the Appendix. The orthogonality assumption between permanent and transitory earnings in equation (1) implies that moment restrictions of the full model are the sum of moment restrictions for permanent and transitory earnings. We use Equally Weighted Minimum Distance which does not weight the minimization problem but adjusts parameter variance post estimation using the empirical fourth moments matrix (see, for example, Haider, 2001).
    ${ }^{11}$ As explained in the data section, we focus on the first two brothers because third or younger brothers are a tiny proportion (4 percent) in the population of families with more than two male sons.

[^8]:    ${ }^{12}$ Parameter estimates of the time effects on both components are reported in Table A1 of the Appendix.

[^9]:    ${ }^{13}$ Estimating the model imposing zero cross-component covariances yielded estimates of the variances of community effects that were statistically significant and of about the same size as the covariances in the unconstrained model.

[^10]:    ${ }^{14}$ Using a model without community effects, Bingley and Cappellari (2013) report an average sibling correlation of 0.23 between ages 25 and 48. Using our sample to estimate a model without community effect in the 25-48 age range we obtain an average sibling correlation of 0.25 . Differences between the two estimates are due to the different age range investigated, different specifications and different sample selections.

[^11]:    ${ }^{15}$ The ratio between neighbor and sibling correlations was 0.47 in Page and Solon (2003).

[^12]:    ${ }^{16}$ More than three quarters of individuals in our sample (76.5\%) do not change parish of residence between ages 14 and 18 , and an additional $22 \%$ changed parish of residence only once or twice. We cannot apply a similar definition to schools because of compulsory schooling ending typically when individuals are aged 15.

